

Direct prediction of HP sequences of compact polymer chains from elastic force

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Abstract

In this paper, a new method is proposed to predict HP sequences of compact polymer chains from elastic force based on the PERM (pruned-enriched-Rosenbluth method) simulation. Two different HP sequences are selected here, and we let them pass through a nanopore after acting of elastic force, which only allow single but not double strands to pass. Some thermodynamics properties of compact polymer chains are investigated during the translocation process, such as average Helmholtz free energy $\langle A \rangle$, average energy per bond $\langle U \rangle$, and average contact energy per bond $\langle U_c \rangle$. We find that the curves of them change non-monotonously with different steps, which inversely can be used to distinguish H and P accurately. The most important parameter of them is elastic force f because it can be measured directly using single-molecule force spectroscopy (SMFS) in experiment. Through recording and comparing force-extension curves, we can determine the HP sequences accurately. This method is also applied to determine DNA sequence directly, and to study the contact interactions in proteins and the protein folding.

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1. Introduction

There are a series of recent experiments and theories to study the translocation of DNA, RNA molecules and proteins through narrow pores, which allow single but not double strands to pass [1–10]. Actually, biopolymers translocation across a nanopore or into membranes is ubiquitous in biosystems. Examples include the viral injection of DNA into a host, the invasion of RNA viruses into healthy cell [11], the translocation of RNAs across a nuclear membrane after their synthesis [12], the incorporation of membrane proteins into lipid bilayers [13], and the electric-field-induced migration of DNA through an α -hemolysin protein channel in membrane [7,8]. There are similar macromolecular transport mechanism such as drug delivery and gene therapy [14] in biotechnology where it is fundamental to understand how DNAs can be incorporated into cell. Understanding of the behavior of biopolymers during the translocation process will make us better to explain varieties of biological phenomenon and we

can use it in practice to serve us, for example, if we know the whole process of RNA viruses transport into healthy cell, we can try to prevent the translocation process and the advent of the disease.

Recently, experiments are motivated by the possibility to read off the sequence of a DNA or RNA by making it pass through a pore [7–10,15–17]. In the experiment, α -hemolysin and a membrane protein were used as the pore, if the pore is small enough that allows only single but not double strands to pass then it can be used as a single-molecule tool, the significance of which is that single-molecule force spectroscopy (SMFS) [18] based on atomic force microscopy (AFM) [19] is becoming a useful tool to study intermolecular and intra-molecular interactions with its extremely high force sensitivity. In contrast, many theoretical studies have shed light on the dynamics of the translocation process [2–6], until very recently [1], Gerland et al. used the pore to unzip basepaired regions in polynucleotide during the translocation process. Actually, the pore plays a very important role in the translocation of structured polymers, as schematically depicted in Fig. 1. In Fig. 1, two processes of unzipping the contacts in a compact polymer are very different, for example, by pulling on its ends we cannot judge the sequence of contact unzipping, but by passing through a pore the contacts will unfold in a linear order along the sequence.

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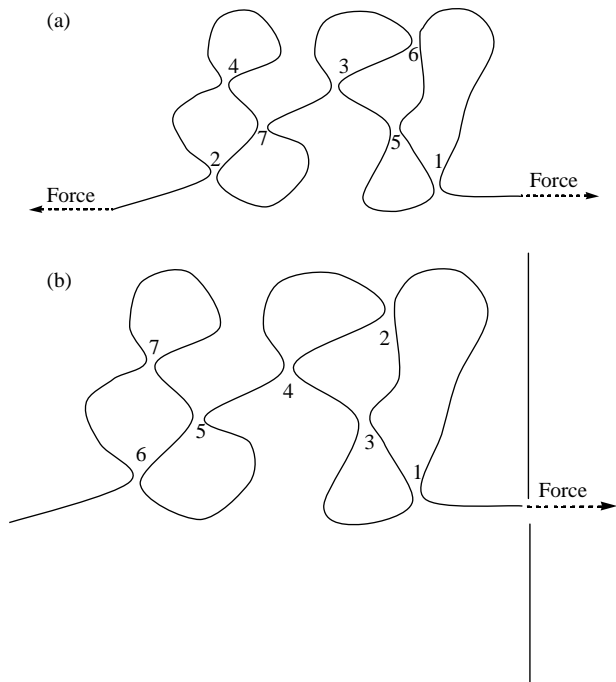


Fig. 1. Two different behaviors of compact polymer chain by pulling on its two ends and by driving it through a nanopore. (a) For pulling on its two ends, the contacts of the chain unzip in an order according to their relative stability and the interior structure, a possible unzipping order 1–7 is indicated. (b) In contrast, the nanopore forces the contacts to unfold along the sequence of the chain, and the order of 1–7 is indicated.

According to this model, here we will discuss something about reading off the HP sequence of compact polymer chain from pulling compact polymer chains through nanopore. By acting a force on compact polymer chain for the translocation and recording force spectrum achieved by AFM, we can determine the HP sequence of compact polymer chains accurately. Of course, this prediction of the HP sequence is now made in theory not in experiments.

2. Model of simulation

In order to simulate the translocation process, we consider a compact polymer chain on cubic lattice, and the chain is adsorbed on the surface near the nanopore and then it is pulled through the nanopore, which is depicted schematically in Fig. 2. Of course, the chains may be away from the surface if the interactions between monomers and attractive surface are weak. In this paper we use the HP lattice model that was proposed by Dill and his cooperators [20,21], and in this model, 20 different amino acids in real proteins are simply divided into two types of amino acids according to the interactions between amino acids and water, i.e. hydrophobic (H) and hydrophilic (P). In the HP model, there is a strong mutual pair-wise attraction between H monomers, and the H monomers can form strong contacts while H–P and P–P monomers can not form any contact, and generally, the values can be employed $\varepsilon_{HP} = \varepsilon_{PP} = 0$, $\varepsilon_{HH} = -1$ (in the unit of $k_B T$) [21–23]. In this paper, we suppose the adsorption surface is hydrophobic, i.e. only the H

monomers have adsorption interaction with the surface, which could be done in experiment [24]. With the purpose of discriminating H and P according to the force spectrum we employ the adsorption energy of H and P as $\varepsilon_H = -3$ and $\varepsilon_P = 0$, respectively. The Hamiltonian of compact polymer chain system with adsorption interaction can be defined as:

$$E = \sum_{i < j} \varepsilon_{ij} \Delta(r_i - r_j) + V \quad (1)$$

here ε_{ij} is the contact energy between monomers i and j , and $\varepsilon_{HP} = \varepsilon_{PP} = 0$, $\varepsilon_{HH} = -1$ [21–23]. $\Delta(r_i - r_j) = 1$ if r_i and r_j are adjoining lattice sites with i and j not adjacent along the chain, while $\Delta(r_i - r_j) = 0$ otherwise [23]. Compact polymer chain is an important conformation because it is the principal configurations of globular proteins. In the meantime, the additional item V in Eq. (1) represents the adsorption interaction, which is defined as:

$$V = \begin{cases} \varepsilon_H & \text{for H monomers on the surface} \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

In this paper, the pruned-enriched-Rosenbluth method (PERM) [25] is adopted to calculate the thermodynamic properties of compact chains on cubic lattice. Grassberger had used this algorithm to simulate flexible chains and their results can illustrate that this method is the most efficient for three-dimensional polymers on the simple-cubic lattice. In our model, the first monomer of compact chain will start at the continuous lattice position along x -axis, i.e. along the pore direction that is vertical to the surface, as shown in Fig. 2, and the chain is pulled at different position a and a' , respectively. If the pulling force is strong enough, the shape of the polymer can be stretched completely [2]. Under this condition, the part of polymer chain that has been pulled through the nanopore is quite stretched, like a directed random walk. According to Kantor's model [2], we suppose the part of compact chain that has been pulled through the nanopore cannot form contacts,

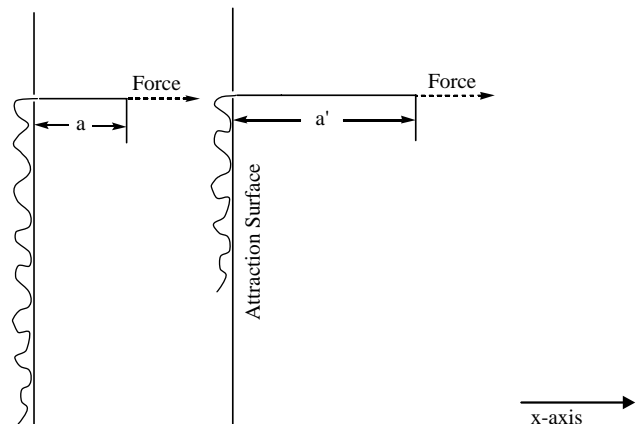


Fig. 2. A HP compact polymer chain adsorbed on the surface is driven through a nanopore by force. Here we suppose that only the H monomers have adsorption interaction with the attractive surface, i.e. the surface is hydrophilic, and the adsorption energy of H and P monomers between the monomers and the surface is $\varepsilon_H = \varepsilon_{att} = -3$ and $\varepsilon_P = 0$, respectively.

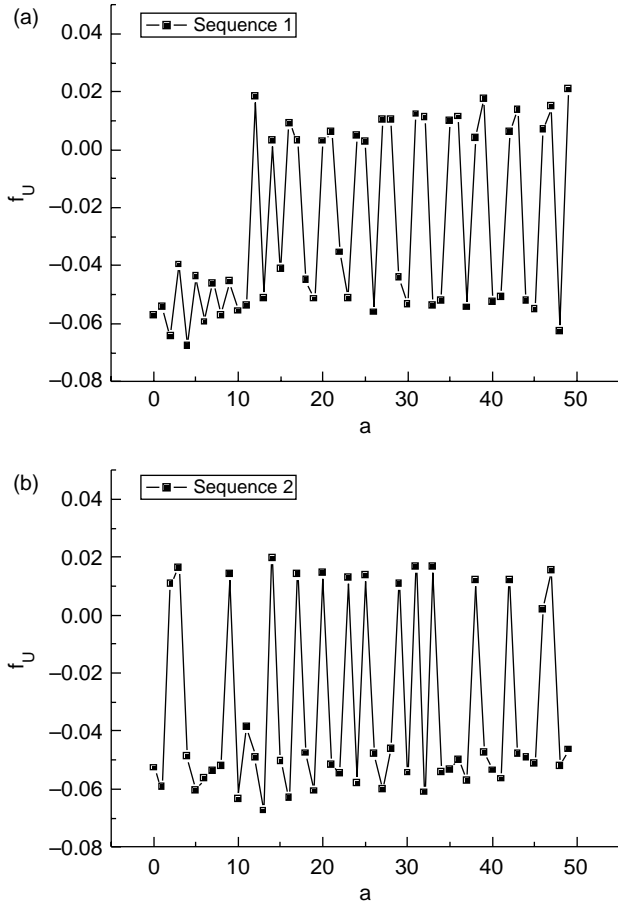


Fig. 8. Energy contribution to force per bond f_u as a function of a during the translocation process. (a) sequence 1: HHHHHHHHHHHHHHPHH; and (b): sequence 2: HHP.

Here $S_i = \text{col}(x_i, y_i, z_i)$ is the position of monomer i in a frame of reference with its origin at the center of a chain. The tensor S can be diagonalized to be a diagonal matrix with three eigenvalues L_1^2, L_2^2 and L_3^2 ($L_1^2 \leq L_2^2 \leq L_3^2$). Actually, Solc and Stockmayer had used these parameters to measure the shape of flexible polymer chains [34,35], and they estimated the ratio $\langle L_1^2 \rangle : \langle L_2^2 \rangle : \langle L_3^2 \rangle$ to be 1:2.7:11.7 based on a random walk of 100 bonds on a simple cubic lattice using Monte Carlo (MC) technique. According to the three eigenvalues from Eq. (7), another important parameter [36,37] of the shape of compact polymer chains can be obtained by combining the reduced components to a single quantity that varies between 0 (sphere) and 1 (rod), and it is defined as:

$$\langle \delta \rangle = 1 - 3 \left\langle \frac{L_1^2 L_2^2 + L_2^2 L_3^2 + L_1^2 L_3^2}{(L_1^2 + L_2^2 + L_3^2)^2} \right\rangle \quad (8)$$

In general, mean-square end-to-end distance $\langle R^2 \rangle$ and mean-square radius of gyration $\langle R^2 \rangle$ are important parameters to illuminate the dimensions of compact polymer chains, but in this paper as the part of chains pulled through the nanopore are in a straight line and cannot form contacts anymore, therefore

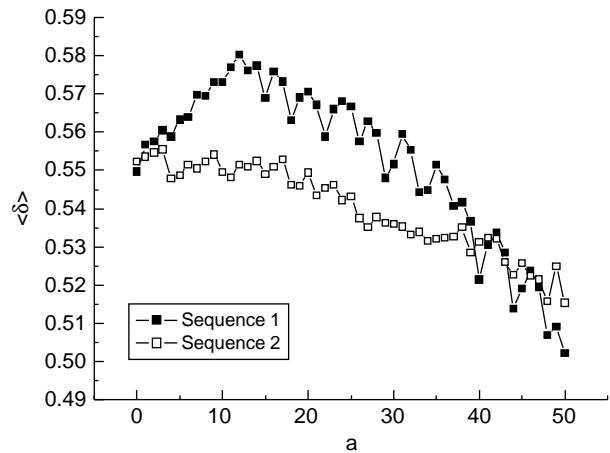


Fig. 9. $\langle \delta \rangle$ as a function of a during the translocation process. Sequence 1: HHHHHHHHHHHHHHPHH; and sequence 2: HHP.

$\langle R^2 \rangle$ and $\langle S^2 \rangle$ become meaningless, as well as, our major purpose is to predict the HP sequence of the chains according to the force spectrum. So here we only consider the shape factor $\langle \delta \rangle$ and it as a function of a during the translocation process is shown in Fig. 9. As we all know, the value of $\langle \delta \rangle$ for general compact polymer should be zero because it is a completely sphere and generally, the $\langle \delta \rangle$ will be asphericity [38]. For example, when compact polymer chains are adsorbed on the attractive surface, they will be compressed by the surface and their shapes are not sphere anymore, and at the beginning of the translocation process, the chains are adsorbed on the surface near the nanopore and the values of $\langle \delta \rangle$ are 0.549 and 0.552 ($a=0$). As the chains are pulled through the nanopore, the value of $\langle \delta \rangle$ decreases gradually, and it becomes 0.502 and 0.515, respectively, after 50-monomer passing through the nanopore. However, we can see from Fig. 9, for sequence 1 the values of $\langle \delta \rangle$ increase monotonously from $a=0$ to 10, and then the values decrease as a whole but locally increase just as the whole change of sequence 2. From $a=0$ to 10 there are all H monomers for sequence 1, so the values of $\langle \delta \rangle$ will change steadily, while there some P monomers in sequence 2 from $a=0$ to 10, so the values will change wavyly. In fact, after 50-monomer pulling through the nanopore, it is in a straight line and the rest parts of the chains are also adsorbed on the surface near the pore.

In this paper we perform the pruned-enriched-Rosenbluth method (PERM), to study the translocation process of three-dimensional adsorbed compact polymer chains. The pore here is used as a tool to unzip the contacts in the chains, and we mainly investigate some thermodynamic properties of compact polymer chains in order to predict the sequence of unknown HP chains using these thermodynamic parameters. The most important parameter is the elastic force because this parameter can be measured directly by atomic force microscope (AFM) in experiment. If we can find the relationship between the sequence of unknown HP chain and elastic force in theory,

we therefore can determine the sequence accurately through investigating the force spectrum of the chains recorded by AFM. In a word, our method is also a useful tool to study protein folding both in theory and in experiment. On the other hand, we may use this method to predict unknown DNA sequence. The HP lattice model used in our simulation is very rough. In this model, 20 amino acid residues of proteins are divided into two types, i.e. hydrophobic and hydrophilic, which omits the other differences between these amino acids, and so far in real experiment we can not use this model. However, it is an important model for studying protein conformations and protein folding [21–23,39–44]. Here we propose a feasible idea to predict the sequence of HP chains with the hope of doing it in experiment someday, and it is also expected that this model can be used to predict the sequence of DNA and make it into practice in the future.

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